

$$t_{cool} \equiv \frac{E}{\dot{E}} \sim \frac{\frac{3}{2} \rho k_B T}{\mu \Delta(T)}$$

$$\tau_{dyn} \sim \frac{R}{v} \left[\frac{2GM}{R^3} \right]^{-1/2}$$

$$t_{cool} \sim 8 \times 10^6 \text{ yr} \left(\frac{\rho}{1 \text{ cm}^{-3}} \right)^{-1}$$

$$\cdot \left[\left(\frac{I}{10^6 \text{ K}} \right)^{-1/2} + 1.5 f_m \left(\frac{I}{10^6} \right)^{-1} \right]$$

f_m ↑ Bremsstrahlung ← lines
f-f f-b
 b-b

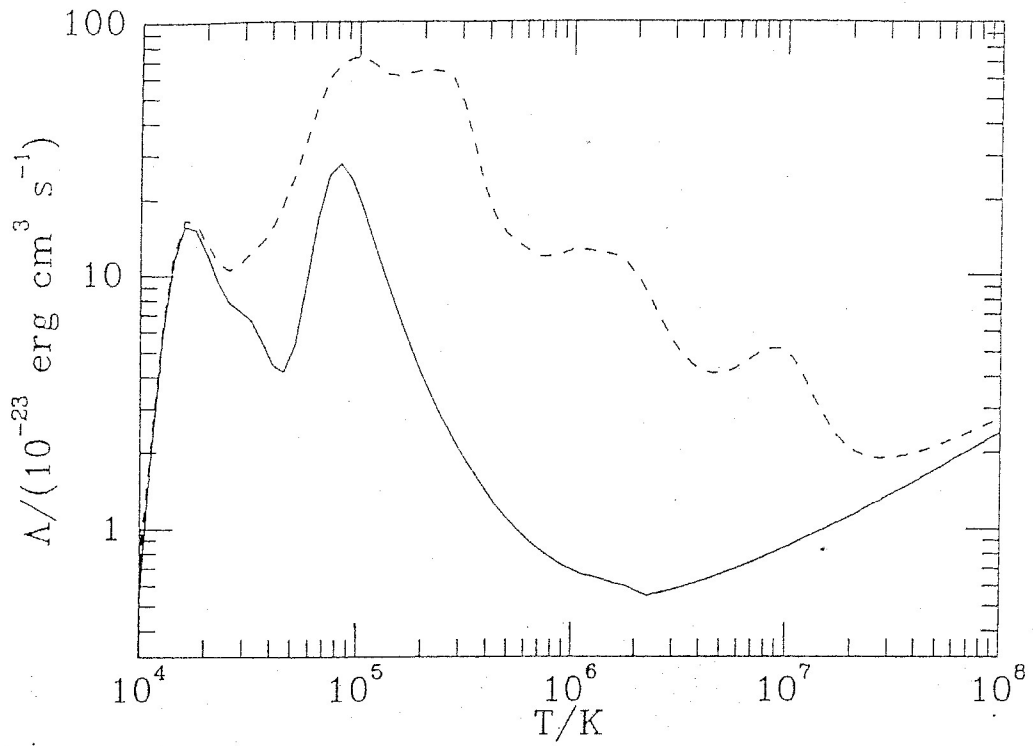
$f_m \sim 1$ Primordial, no metals

$f_m \sim 30$ solar abundance

For $T < 10^6$, $f=1$, $M=0.57$

$$\tau = \frac{t_{cool}}{\tau_{dyn}} \sim \frac{M}{9 \times 10^{-11} M_{\odot}}$$

$\rightarrow M_{gal} \lesssim 10^{12} M_{\odot} \quad | \quad \tau_{tot} \rightarrow R \sim 80 \text{ kpc}$
 total mass



$$1D \sigma_v (= [kT/\mu m_p]^{1/2}) / \text{km s}^{-1}$$

