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Vertical loop nodes in iron-based superconductors

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We consider Fe-based superconductors with s^{+-} gap with accidental nodes on electron pockets. We analyze how the gap structure changes if we include into the consideration the hybridization between the two electron pockets [the interpocket hopping term with momentum (π,π,π)]. We derive the hybridization term and relate it to the absence of inversion symmetry in the Fe plane because of two nonequivalent locations of pnictogen (chalcogen) above and below the plane. We find that the hybridization tends to eliminate the nodes—as it increases, the pairs of neighboring nodes approach each other, merge, and disappear once the hybridization exceeds a certain threshold. The nodes disappear first around $k_z = \pi/2$, and vertical line nodes split into two vertical loops centered at $k_z = 0$ and $k_z = \pi$. We also show that the hybridization moves the nodes along the loops away from the normal-state Fermi surfaces. This creates a subset of k points at which the peak in the spectral function does not shift as the system enters into a superconducting state ("no-shift" lines). These no-shift lines evolve with increasing hybridization in a highly nontrivial manner and eventually form horizontal loops in the (k_x,k_y) plane, surrounding the nodes. Both vertical line nodes and horizontal no-shift loops surrounding them should be detectable in photoemission experiments.

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I. INTRODUCTION

Understanding high-temperature superconductivity in doped Fe pnictides and Fe chalcogenides remains the top priority for the condensed-matter community. 1–4 Superconductivity in weakly/moderately doped systems is generally believed to be the consequence of the complex geometry of the Fermi surface (FS), which consists of hole and electron pockets located in different regions of the Brillouin zone. The prevailing scenario is that the superconducting gap has an *s*-wave symmetry, but changes sign between hole and electron pockets, 5,6 and may even have accidental nodes. 1,7

Previous studies of the pairing mechanism and the gap structure in Fe-based superconductors mostly focused on a two-dimensional (2D) model of a single Fe plane with adjacent pnictogen/chalcogen atoms located immediately above and below it. $^{1,6,8-13}$ Electrons from 3d orbitals of Fe hop mostly indirectly, via 4p pnictogen/chalcogen sites. The low-energy structure around E_F obtained from a 3d-4p hopping has been fitted^{1,6,8,11-13} to an effective "Fe only" 2D five-orbital tight-binding Hamiltonian with interorbital and intraorbital hopping terms. The band structure and location of the electron and hole FSs have been deduced by evaluating the eigenvalues of the five-orbital tight-binding Hamiltonian and analyzing the energy profile. The pairing problem can be most straightforwardly analyzed in the band basis, by associating the operators corresponding to eigenfunctions with band operators and rewriting the interaction in the band basis. The band operators are linear combinations of orbital operators, and the interactions in the band basis are the ones in the orbital basis, dressed by "coherence factors" associated with the fact that each eigenfunction is a linear combination of Fe orbitals. The dressed interactions inherit angular dependencies from the coherence factors. Solving for gaps on different FSs, one then generally obtains angular-dependent gaps, even in the s-wave case. By generic reasoning, the s-wave gaps on hole pockets contain $\cos 4n\phi$ harmonics (n = 0, 1, 2...), where ϕ is the angle along the hole pocket, while the gaps on electron pockets contain both $\cos 4n\theta$ and $\cos 2\theta(2n+1)$ harmonics, with the angle θ counted relative to, e.g., the x axis for one pocket and the y axis for the other.^{7,14,15} Numerical analysis shows^{1,14} that $\cos 2\theta$ harmonic of the gap is the strongest one, and in some materials it is large enough to induce accidental nodes on electron FSs.

The actual Brillouin zone (BZ), however, contains two Fe atoms because pnictogen/chalcogen is located below and above the Fe plane in checkerboard order (see Fig. 1). The positions of pnictogen/chalcogen atoms are shifted by half of lattice spacing in both x and y directions relative to the positions of Fe. Half of pnictogen/chalcogen atoms are located above the Fe plane and half are located below the Fe plane. As a consequence, for half of the Fe atoms hopping to pnictogen/chalcogen means hopping down along z and for the other half it means hopping up along z. Therefore, the symmetry of the original lattice is lower than the symmetry of the Fe lattice, and the effective tight-binding Hamiltonian should generally contain two type of terms—the ones with zero momentum transfer, and the ones with momentum transfer $Q = (\pi, \pi)$ (Refs. 16 and 17) (here and below we set interatomic spacing to 1).

The tight-binding Hamiltonian considered in earlier studies¹ includes only the terms with zero-momentum transfer. For such a Hamiltonian, the transformation from the 1-Fe BZ to the 2-Fe BZ is just a rotation in a momentum space: momenta k_x and k_y from the 1-Fe zone are transformed into $\tilde{k}_a = k_x + k_y$ and $\tilde{k}_b = k_x - k_y$ in the 2-Fe zone. The gap structure is obviously not affected by this transformation, up to a change of variables. In particular, if the gap has accidental nodes in the 1-Fe zone, it will have accidental nodes in the 2-Fe zone as well.

In this paper we demonstrate that the effective tight-binding Hamiltonian also contains hopping terms with momentum transfer Q, and that these terms affect the physics in a

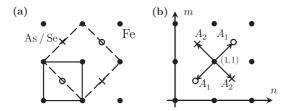


FIG. 1. (a) Schematic representation of a single layer of pnictide/chalcogenide. The solid square designates a Fe (solid circles) only lattice unit cell. The As/Se atoms form two inequivalent subsets. The atoms denoted by a cross and empty circles are shifted off the Fe plane in opposite directions. (b) The hopping amplitudes to a neighboring pnictogen/chalcogen site are generally different for pnictigen/chalcogen above and below Fe plane, i.e., in general $A_1 \neq A_2$.

quantitative way, and, in particular, substantially modify the gap structure. The (π,π) term vanishes if one approximates a 2D five-orbital model by just d_{xz} and d_{yz} orbitals, as has been done in some earlier studies 11,18 but is present once one adds a d_{xy} orbital (the (π,π)) term describes the hopping from d_{xy} orbital to d_{xz} or d_{yz} orbital). Because the low-energy hole and electron states in the full 2D tight-binding Hamiltonian have contributions from d_{xz} , d_{yz} , and d_{xy} orbitals, $^{1,6,8-10,12,13,19}$ the (π,π) hopping term survives the transformation to band formalism and becomes $\psi_k^{\dagger} \psi_{k+Q}$, where ψ are band operators. As the two electron FSs are separated exactly by Q, such term gives rise to a hybridization between the two electron pockets. The new band operators for low-energy fermions then become a linear combination of the original ψ_k , and the pairing interaction, re-expressed in terms of the new band operators, acquires additional coherence factors, which modify its angular dependence. The modification of the angular dependence of the interaction in turn modifies the angular dependence of the gaps on electron FSs. This physics must be present in ten-orbital studies, 9,10,19 which treat orbital excitations with momentum k and k + Q as separate degrees of freedom, but we are not aware of the attempt to fit the results of ten-orbital numerical studies by an effective tight-binding Hamiltonian with an additional (π,π) term.

In the previous work²⁰ we demonstrated that hybridization plays a crucial role in systems with only electron pockets, like KFe₂Se₂. Several groups analyzed the pairing problem in KFe₂Se₂ in the absence of hybridization. If the interaction between the two electron pockets is repulsive, the pairing is possible if interpocket interaction exceeds intrapocket repulsion, but the gaps on the two electron pockets should have opposite signs. 14,21,22 Such a state has a d-wave symmetry because the gap changes sign under rotation by 90°. The hybridization mixes the two original electron pockets into two new electron pockets; each contains states from both original pockets. The two new pockets split upon hybridization, and the solution of the pairing problem for strong enough hybridization shows that the system prefers to form an s-wave gap with opposite sign on the two hybridized FSs. 17,20 In terms of original fermions the condensate wave function for such an s-wave state is made out of fermions from different electron FSs, i.e., a pair has a momentum Q. In terms of new, hybridized fermions, such a state is a conventional one, with zero total momentum of a pair. The microscopic analysis of the pairing

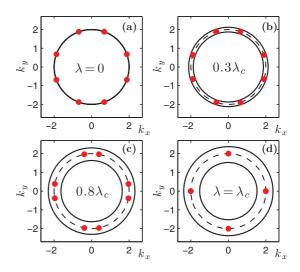


FIG. 2. (Color online) Evolution of the FS and gap nodes shown by (red) dots for circular pockets and constant (angle independent) hybridization amplitude. Without hybridization, the two electron FSs are identical, and each has four nodes (a). Once the hybridization parameter λ becomes nonzero, the two electron FSs split, but the nodes remain on the original (nonhybridized) FS (b),(c). As λ increases, the pairs of neighboring nodes come closer to each other and eventually merge at λ_c (d) and disappear at larger λ . We set $\alpha=1.3$.

in the presence of hybridization shows²⁰ that, with increasing hybridization, the system undergoes a two-step transition from a d-wave state to a $d \pm is$ state and then to an s^{+-} state.

In this paper we analyze the role of hybridization in systems in which both hole and electron pockets are present and the gap has s^{+-} form. We take the gap structure from the 2D tight-binding Hamiltonian without Q terms as an input and analyze how it changes once we add additional hopping with momentum transfer Q. At first glance, the hybridization between the two electron pockets should not lead to qualitative changes in the s^{+-} gap because the gaps' order parameter on these pockets on average have the same sign. We show, however, that the actual situation is more tricky and hybridization does give rise to qualitative changes in the gap structure in systems like $BaFe_2(As_{1-x}P_x)_2$, ²³ LaOFeP, ²⁴ and LiFeP, 25 in which the s^{+-} gap has accidental nodes, which most likely reside on electron pockets. By symmetry, there are four nodes on each electron pocket (eight nodes in total). We show that the hybridization brings the neighboring nodes close to each other. When the hybridization reaches a certain threshold, the nodes coalesce and disappear (see Figs. 2 and 4). The importance of hybridization between electron pockets was recognized in Ref. 10. The authors of that work conjectured that it may affect the location of the gap nodes. Our explicit calculations do show that the nodal structure is indeed affected by hybridization.

We follow the evolution of the nodes before the hybridization reaches a threshold. We show that at any nonzero hybridization the nodes do not reside on the normal-state FSs but are shifted into the k region between the hybridized FSs, where the angle-resolved photoemission spectroscopy (ARPES) intensity above T_c is peaked at a finite negative frequency. As a result, the peak in the ARPES spectra at

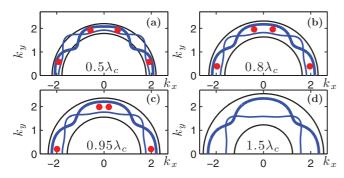


FIG. 3. (Color online) Location of the NSL, defined as locus of points for which fermion does not change its energy between the normal and the superconducting states. Thick (blue) lines are NSLs which are detectable by ARPES (the peaks above and below T_c are located at the same negative energy), thin (blue) lines are NSLs for which the peak above T_c is at a positive energy. The hybridization parameter λ increases from (a) to (d). Dots (red) are nodal points at which quasiparticle energy is zero in a superconductor (but not in the normal state). The initial evolution of NSLs is quite involved. We consider it in Appendix B.

the nodal point does not stay intact, as in a "conventional" superconductor with gap nodes, but shifts towards a smaller frequency below T_c . We further show that each nodal point is surrounded by no-shift lines (NSLs), at which quasiparticle energies in the normal and superconducting states are equal, i.e., the peak in the ARPES spectrum does not shift when the system becomes a superconductor (Figs. 3 and 4). Without hybridization, these NSLs are radial beams transverse to the FS, in the direction along which the gap vanishes. Upon hybridization, NSLs rapidly evolve, rotate by 90°, and transform into loops directed *along* the FSs. Inside the loop, the ARPES peak moves to a lower negative frequency below T_c , outside the loop it moves to a higher negative frequency. We propose to search for such NSLs in ARPES measurements

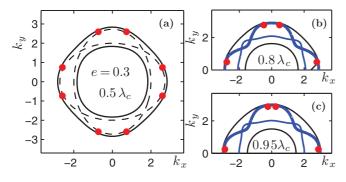


FIG. 4. (Color online) Hybridization of 2D elliptical FSs. (a) FSs and the location of nodes (red dots). Solid and dashed black lines are the actual, hybridized FSs, and the original FSs, respectively. Similarly to the case of circular FSs, the pairs of nodal points come closer to each other as λ increases, and merge and disappear at a critical λ_c . (b), (c) Evolution of the NSL with increasing λ . Solid black lines show the hybridized FSs. Thick and thin solid blue lines are NSLs detectable and undetectable by ARPES, respectively. The 2D analysis is applicable to 1111 materials with simple tetragonal lattice structure. For 122 materials with body-centered lattice structure, the situation is somewhat different; see Fig. 5.

on BaFe₂(As_{1-x}P_x)₂ and other s^{+-} superconductors with gap nodes, like LaOFeP (Ref. 24) and LiFeP.²⁵

We next consider the effect of hybridization in 3D systems. For 1111 systems with a simple tetragonal lattice, the hybridization term has 3D momentum $(\pi, \pi, 0)$, 3D effects are secondary, and the consideration is qualitatively the same as in 2D systems. In 122 systems with body-centered-tetragonal lattice, the situation is more interesting. We show that in these systems the hybridization between electron pockets is three dimensional, with hybridization vector (π, π, π) , even if we neglect the k_z dependence of the gap along the third direction within the 1-Fe tight-binding Hamiltonian.²⁶ This is due to the fact that in 122 materials pnictogen/chalcogen atoms alternate in checkerboard order between neighboring Fe planes, i.e., if for a given Fe plane a pnictogen/chalcogen atom at a given (x,y) is located above the Fe plane, then in the neighboring Fe plane a pnictogen/chalcogen atom at the same (x, y) is located below the Fe plane.²⁷ We show that, for such a structure, the hybridization term has 3D momentum $Q = (\pi, \pi, \pi)$, and is the largest at $k_z = \pi/2$ (it actually does not vanish, except for $k_z = 0$ and $k_z = \pi$, even if we consider only d_{xz} and d_{vz} Fe orbitals). We show that, at the same time, the critical value of the hybridization, at which the nodes disappear, is the smallest at $k_z = \pi/2$ and is much larger for $k_z = 0$ and $k_z = \pi$. The combination of the facts that at $\pi/2$ the value of the hybridization is the highest and the threshold value is the lowest implies that there must be a wide range of hybridizations when the nodes are eliminated near $\pi/2$ but are still present near $k_z = 0$ and $k_z = \pi$. In this range vertical line nodes close up into vertical loop nodes centered at $k_z = 0$ and $k_z = \pi$ (see Fig. 5). The gap structure with such loop nodes has been proposed phenomenologically²³ as the best candidate to fit the thermal conductivity data in BaFe₂($As_{1-x}P_x$)₂, for which penetration depth, thermal conductivity, specific heat, and NMR data all show²⁸ that the gap must have nodes, and at least some ARPES results²⁹ indicate that the nodes must

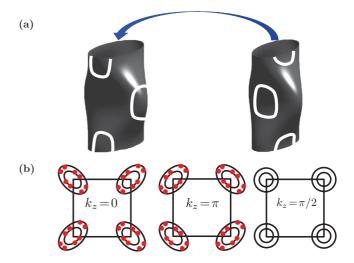


FIG. 5. (Color online) (a) 3D FSs of 122 systems, like $BaFe_2(As_{1-x}P_x)_2$, and the location of vertical loop nodes shown by white lines. Two warped cylinders are shown separately, but the smaller one is actually inside the larger one, as the arrow indicates. (b) Cross section of the actual FSs at various k_z . Red dots mark the location of the nodes.

be on the electron FSs. Our result provides a microscopic explanation of vertical loop nodes.

The paper is organized as follows. In the next section we present the model of a s^{+-} superconductor with nodes on electron pockets and introduce the hybridization amplitude. In Sec. III we discuss how the hybridization affects the nodes of the superconducting gap in systems with a simple tetragonal lattice structure. We consider first a toy model with circular electron pockets and then consider a more realistic model of elliptical pockets. We show that in both cases the neighboring nodes move towards each other as hybridization amplitude increases. In Sec. IV we extend the analysis to a 3D body-centered-tetragonal lattice and show that hybridization splits vertical line nodes into vertical loop nodes centered at $k_z = 0$ and $k_z = \pi$. In Sec. V we discuss the experimental situation and comment on recent ARPES studies of the superconducting gap structure in BaFe₂(As_{1-x}P_x)₂. We present our conclusions in Sec. VI. We discuss technical issues in detail in three Appendixes. In Appendix A, we discuss in detail the microscopic mechanism of hybridization in 2D and 3D lattices and obtain explicit expressions for the hybridization amplitude for a simple tetragonal lattice structure and for a body-centered-tetragonal lattice structure. In Appendix B we discuss the evolution of NSLs from radial beams in the direction transverse to the FS along which the gap vanishes to closed loops directed along the FSs. In Appendix C we discuss subtleties in extracting the positions of gap nodes from ARPES data.

II. MODEL

We consider an s^{+-} superconductor with two electron pockets at $(0,\pi)$ and $(\pi,0)$ in the 1-Fe BZ at any given k_z , and the appropriate number (2 or 3) of hole pockets centered at (0,0). The actual pocket structure in Fe-based superconductors is somewhat more involved, i.e., low-energy states near $(0,\pi)$ and $(\pi,0)$ likely contain not only electron pockets centered at these points, but also hole barrels, centered somewhat away from $(0,\pi)$ and $(\pi,0)$. These hole barrels will not play a role in our consideration and we neglect them.

In the absence of hybridization, the quadratic part of the Hamiltonian for electron pockets is

$$H_2 = \sum_{k} \xi_{1,k} \psi_{1,k}^{\dagger} \psi_{1,k} + \xi_{2,k+Q} \psi_{2,k+Q}^{\dagger} \psi_{2,k+Q}, \qquad (1)$$

where $\psi_{1,2}$ describe two electron bands, one with low-energy excitations near $\mathbf{k}_1=(0,\pi)$, and another with low-energy excitations near $\mathbf{k}_2=(\pi,0)=\mathbf{k}_1+\mathbf{Q}$ (modulo 2π), $\xi_{1,k}$ and $\xi_{2,k+\mathbf{Q}}$ are the corresponding electron dispersions, and $\mathbf{Q}=(\pi,\pi)$. We approximate fermion excitations near the pockets by $\xi_{1,k}=v_F(\theta)[|\mathbf{k}-\mathbf{k}_1|-k_F(\theta)], \xi_{2,k+\mathbf{Q}}=v_F(\theta+\pi/2)[|\mathbf{k}-\mathbf{k}_2|-k_F(\theta+\pi/2)],$ where θ is the angle along each of the FSs counted from the x axis. $^{1-3,20}$ By virtue of tetragonal symmetry, $v_F(\theta)=v_F(1+a\cos2\theta)$ and $k_F(\theta)=k_F(1+b\cos2\theta)$. The parameter b accounts for the eccentricity (ellipticity) of the FSs. For 1111 systems, parameters a and b are essentially independent on k_z , and one can reduce the analysis to the 2D model. For 122 systems a and b do depend on b_z and change sign and magnitude between $b_z=0$ and $b_z=\pi$.

We assume, following earlier works, ^{1–4,6} that the dominant pairing interaction is between electrons and holes, and that its dependence on k_z is weak and can be neglected. We follow Refs. 7, 14, and 15 and approximate electron-hole interaction by a constant term and by a $\cos 2\theta$ term, which changes sign between the two electron pockets. Within this approximation, the gaps on hole FSs are angle independent, while the gaps on the two electron FSs are $\Delta(1 \pm \alpha \cos 2\theta_k)$. The corresponding effective BCS Hamiltonian is

$$H_{BCS} = \Delta \sum_{k} [(1 - \alpha \cos 2\theta_{k})\psi_{1,k}\psi_{1,-k} + \text{H.c.}] + [(1 + \alpha \cos 2\theta_{k})\psi_{2,k+Q}\psi_{2,-k-Q} + \text{H.c.}].$$
 (2)

We consider the case $\alpha > 1$, when the gaps have accidental nodes in the absence of hybridization between the two electron pockets. The hybridization term in the 1-Fe BZ has the form

$$H_{Q} = \sum_{k} \lambda(k) \psi_{1k}^{\dagger} \psi_{2,k+Q} + \text{H.c.}$$
 (3)

We present the derivation of Eq. (3) in Appendix A for both 2D and 3D systems. We show there that the prefactor $\lambda(k)$ is generally a complex number, which depends on both k_z and k_{\perp} . When only the d_{xz} and d_{yz} orbitals of Fe are considered, the hybridization vanishes completely in the 2D case and along particular directions in the 3D case. The k dependence becomes less strong once one adds into consideration the d_{xy} orbital along with spin-orbit interaction. In the latter case, $|\lambda(k)|$ does not vanish for any k, although it is smaller at $k_z = 0$ and along $k_x = \pm k_y$ measured from the center of one of the electron pockets. The nonsingular k dependence of $\lambda(k)$ is not essential to our analysis, and to simplify the presentation we approximate $\lambda(k)$ by a constant λ for the rest of the paper. Our goal is to analyze what happens with the nodes, and, more generally, with the fermion dispersion, when we solve for the pairing in the presence of the hybridization term.

III. EFFECT OF HYBRIDIZATION ON NODES, 2D CASE

In this section we consider the case of a simple tetragonal lattice for which the pairing problem can be analyzed within a single 2D cross section (we recall that we treat interactions as independent on k_z). In the presence of H_Q , Eq. (3), the quadratic part of the Hamiltonian for fermions near the two electron FSs becomes, instead of (1),

$$H_{2} = \sum_{k} \xi_{1,k} f_{1,k}^{\dagger} f_{1,k} + \xi_{1,k+Q} f_{2,k+Q}^{\dagger} f_{2,k+Q} + \sum_{k} \lambda [f_{1,k}^{\dagger} f_{2,k+Q} + \text{H.c.}].$$
(4)

For convenience, we redefine k and count it relative to $k_1 = (0,\pi)$ for f_1 fermions and relative to $k_2 = (\pi,0)$ for f_2 fermions, i.e., absorb Q into new k. In these new notations, the quadratic Hamiltonian becomes

$$H_2 = \sum_{j=1,2} \sum_{k} \xi_{j,k} f_{j,k}^{\dagger} f_{j,k} + \sum_{k} \lambda [f_{1,k}^{\dagger} f_{2,k} + \text{H.c.}]. \quad (5)$$

To analyze the pairing, we now have to introduce new fermions which diagonalize the quadratic form in Eq. (5), reexpress the pairing interaction in terms of these new fermions,

and solve for the gaps on electron FSs and quasiparticle dispersion. We start with the case of circular electron pockets, and then extend the analysis to elliptical pockets.

A. Circular electron pockets

For circular pockets, $\xi_{1,k} = \xi_{2,k} = \xi_k = v_F(k - k_F)$ is independent on the angle along the FS. The quadratic part of the Hamiltonian is diagonalized by the transformation to new operators a and b via $f_{1,2} = (a \mp b)/\sqrt{2}$ and becomes

$$H_2 = \sum_{k} \xi_k^+ a_k^{\dagger} a_k + \sum_{k} \xi_k^- b_k^{\dagger} b_k \tag{6}$$

with $\xi_k^{\pm} = \xi_k \pm \lambda$. For angle-independent λ , the new FSs remain concentric circles with different radii.

The BCS Hamiltonian takes the form

$$H_{BCS} = \Delta \sum_{k} \{ (a_{k}a_{-k} + b_{k}b_{-k}) + (a_{k}b_{-k} + a_{k}b_{-k})\alpha \cos 2\theta_{k} \} + \text{H.c.}$$
 (7)

We see that, in terms of a and b operators, the $\cos 2\theta$ term measures the strength of interband pairing. As λ increases and the two hybridized FSs become more separated, interpocket pairing becomes less important, and one expects that the angular dependence of the pairing interaction will play a lesser role. This is what calculations show, as we demonstrate below.

The quasiparticle dispersion is obtained from zeros of the inverse propagator $G_{\omega,k}^{-1} = \omega I - M$ with matrix M and a unit matrix I operating in Nambu space $\psi_k = [a_k, a_{-k}^{\dagger}, b_k, b_{-k}^{\dagger}]^{tr}$. We have

$$M = \begin{bmatrix} \xi_{+} & \Delta & 0 & \Delta y \\ \Delta & -\xi_{+} & \Delta y & 0 \\ 0 & \Delta y & \xi_{-} & \Delta \\ \Delta y & 0 & \Delta & -\xi_{-} \end{bmatrix}, \tag{8}$$

where $y = \alpha \cos 2\theta_k$. The nodal points are located at k_n for which det M(k) = 0. Equation (8) gives

$$\det M = 4\Delta^2 \xi_k^2 + \left[\xi_k^2 - \lambda^2 + \Delta^2 (y^2 - 1) \right]^2. \tag{9}$$

We see that the nodes reside on the "bare" FS, $\xi_k = 0$, and their angular position θ_k is set by

$$\cos \theta_k = \pm \frac{\sqrt{\lambda^2 + \Delta^2}}{\alpha \Delta}.$$
 (10)

Equation (10) has eight solutions along a circle (four pairs of nodes near $\theta=0$ and other symmetry-related points $\theta=\pi/2$, $\theta=\pi$, and $\theta=3\pi/2$). As λ increases, the two nodes located, e.g., near $\theta=0$ move toward each other, and at a critical λ_c given by

$$\lambda_c = \Delta \sqrt{\alpha^2 - 1} \tag{11}$$

the neighboring nodes merge along symmetry lines. At larger λ the nodes disappear. We show this behavior in Fig. 2. Observe that the critical λ_c is of order Δ , i.e., is rather small. We will see below that λ_c is much larger when electron FSs are not circular.

In the presence of impurities, the nodes disappear already at λ smaller than λ_c , once the distance between the nodes becomes smaller than some minimum value set by impurity

scattering. ^{31,32} Consider the range $\lambda < \lambda_c$ in more detail. That the nodes are not located on the actual (hybridized) FSs has a profound effect on the ARPES spectrum. In the normal state, the quasiparticle energies are $\xi_k \pm \lambda$, i.e., one energy is positive along $\xi_k = 0$ and the other is negative. Because ARPES intensity is proportional to the Fermi function, ARPES will only detect a negative mode at $\omega = -\lambda$. That the nodes in the superconducting state are located along $\xi_k = 0$ then implies that around these k, the position of the maximum in the ARPES spectra shifts towards a *smaller* frequency as the temperature drops below T_c , instead of staying intact, as at a nodal point of a "conventional" superconductor with gap nodes. At the same time, one can easily make sure that near the larger FS, the ARPES peak shifts to a larger negative frequency below T_c . As a result, there exist lines in k space along which ARPES intensity does not shift upon cooling through T_c (in the Introduction we termed these lines as no-shift lines, or NSLs).

In the absence of hybridization, the NSLs are radial beams along $y = \alpha \cos 2\theta_k = \pm 1$ for which superconducting dispersion $\omega(\mathbf{k}) = -[\xi^2 + \Delta^2(1 \pm y)^2]^{1/2}$ coincides with the normal state dispersion $-\xi$. Once λ becomes nonzero, $\omega(\mathbf{k})$ splits into two branches,

$$\omega_{12}^2 = (\Delta^2 + y^2 \Delta^2 + \xi^2 + \lambda^2) \mp 2\sqrt{S},$$
 (12)

where $S = \xi^2 \lambda^2 + y^2 \Delta^2 (\Delta^2 + \lambda^2)$. We analyzed (12) and found that the NSLs rapidly undergo a series of bifurcations (see Appendix B) and for $\lambda \lesssim \lambda_c$ evolve into bananalike loops located in between the two hybridized FSs and surrounding the actual nodal points (see Fig. 3). The NSLs persist even above λ_c , when the actual nodes disappear, and should be easily detectable by ARPES (at least, in theory).

B. Noncircular Fermi pockets

For noncircular electron pockets the quadratic Hamiltonian (5) is diagonalized by the angle-dependent transformation $f_1 = ua + vb$, $f_2 = -va + ub$, with $(u,v) = (\cos \phi, -\sin \phi)$, and $\cos 2\phi = (\xi_1 - \xi_2)/\sqrt{(\xi_1 - \xi_2)^2 + 4\lambda^2}$, $\sin 2\phi = 2\lambda/\sqrt{(\xi_1 - \xi_2)^2 + 4\lambda^2}$. The diagonalization yields

$$H_2 = \sum_{k} \xi_a a_k^{\dagger} a_k + \sum_{k} \xi_b b_k^{\dagger} b_k,$$
 (13)

with

$$\xi_{a,b} = \frac{1}{2}(\xi_1 + \xi_2) \pm [\lambda^2 + (\xi_1 - \xi_2)^2 / 4]^{1/2}.$$
 (14)

The Nambu matrix M becomes, instead of Eq. (8),

$$\begin{bmatrix} \xi_{a} & \Delta(1+\alpha_{2}) & 0 & \Delta\alpha_{1} \\ \Delta(1+\alpha_{2}) & -\xi_{a} & \Delta\alpha_{1} & 0 \\ 0 & \Delta\alpha_{1} & \xi_{b} & \Delta(1-\alpha_{2}) \\ \Delta\alpha_{1} & 0 & \Delta(1-\alpha_{2}) & -\xi_{b} \end{bmatrix}, (15)$$

where $\alpha_1 = y \sin 2\phi$, $\alpha_2 = y \cos 2\phi$. The location of the nodes is again specified by det M = 0. We have

$$\det M = \Delta^{2} [(\xi_{a} + \xi_{b}) + \alpha_{2}(\xi_{b} - \xi_{a})]^{2} + [\xi_{a}\xi_{b} + \Delta^{2}(y^{2} - 1)]^{2}.$$
(16)

Both terms in Eq. (16) are non-negative and must vanish simultaneously at the locations of the nodes. This sets two

conditions, one on $\xi_{a,b}$ and one on the angle θ_k . Solving the coupled set we find the same behavior as for circular pockets—the eight nodes are located in between the hybridized electron FSs, and the pairs of neighboring nodes move towards each other as λ increases, merge along symmetry directions at a critical λ_c , and disappear at larger λ (Fig. 4). The critical λ_c is given by

$$\lambda_c = (\alpha^2 - 1)^{1/2} \{ [(\bar{\xi}_1 - \bar{\xi}_2)/2]^2 + \Delta^2 \}^{1/2},$$
 (17)

where $\bar{\xi}_1$ and $\bar{\xi}_2$ are dispersions $\xi_{1,k}, \xi_{2,k}$ along one of four symmetric directions $\theta_k = 0$, $\pi/2$, π , or $3\pi/2$, and the value of k is fixed by the condition $\bar{\xi}_1 = \bar{\xi}_2(\alpha-1)/(\alpha+1)$. For elliptical pockets, with $\xi_{1,2} = k_x^2/2m_{1,2} + k_y^2/2m_{2,1} - \mu$, $(\bar{\xi}_1 - \bar{\xi}_2)/2 = \mu e/(1-\alpha|e|)$, where $e = (m_1-m_2)/(m_1+m_2)$ is the eccentricity. If the two FSs were nearly circular but of different radii before the hybridization (as in body-centered-tetragonal 122 systems), i.e., $\xi_{1,k} = k^2/(2m_1) - \mu$, $\xi_{2,k} = k^2/(2m_2) - \mu$, and $m_1 = m(1+\epsilon)$, $m_2 = m(1-\epsilon)$, then $\bar{\xi}_1 - \bar{\xi}_2 = -k_F^2 \epsilon/(m^2)$, where $k_F \approx \sqrt{2m\mu}$. In both cases, λ_c obviously increases when electron pockets becomes nonidentical.

We computed the dispersion by solving $\det[\omega(k) - M] = 0$ and again found that NSL form banana-shaped closed loops around the true nodes. We show the results in Fig. 4. In similarity to the case of circular pockets, NSLs survive even when the actual nodes disappear.

IV. EFFECT OF HYBRIDIZATION ON NODES, 3D BODY-CENTERED-TETRAGONAL LATTICE

In 122 systems with body-centered-tetragonal lattice, two electron pockets coupled by λ are separated by (π,π,π) , where the third component is along the k_z direction. The pairs of pockets at $(0,\pi,0)$ and $(\pi,0,\pi)$ and at $(\pi,0,0)$ and $(0,\pi,\pi)$ are co-axial ellipses, which are well separated even without hybridization. The difference $\bar{\xi}_1 - \bar{\xi}_2$ is then large, and for k_z near 0 and near π the critical λ_c as given by Eq. (17) is large and generally comparable to Fermi energy. On the other hand, at $k_z = \pi/2$, the two electron pockets coupled by λ are identical, and can be well approximated by circles. For these pockets, the critical λ_c is given by Eq. (11) and is quite small, of order Δ . For $\lambda_c(\pi/2) < \lambda < \lambda_c(0,\pi)$, the nodes near $k_z = \pi/2$ are eliminated, and nodal lines form vertical loops, which are centered at $k_z = 0$ and $k_z = \pi$ and close before reaching $k_z = \pi/2$. We show this gap structure in Fig. 5.

V. APPLICATION TO P-CONTAINING PNICTIDES

The three Fe-pnictide materials with hole and electron pockets, for which experimental data strongly suggest the presence of gap nodes, are LaFeOP, with $T_c \le 5$ K (Ref. 24), the family BaFe₂(As_{1-x}P_x)₂ with the highest T_c around 30 K (Ref. 33), and LiFeP with $T_c \le 5$ K (Ref. 25). All three materials contain phosphors. k_z -integrated probes like penetration depth, thermal conductivity, specific heat, and NMR (Ref. 28) all show the behavior consistent with line nodes. In particular, thermal conductivity κ scales linearly with T at low T and displays \sqrt{H} behavior in a magnetic field, and $\lambda(T) - \lambda(0)$ is also linear in T down to very low T.

The results of ARPES study of the gap structure are controversial. Laser ARPES study²⁹ probed the gap near

the three hole pockets and found all of them almost angle independent, at least for k_7 probed by laser ARPES. These authors argued that the nodes must be on electron pockets. Synchrotron ARPES data were, on the other hand, interpreted as evidence for a horizontal line node at some k_7 on one of hole FSs. We argue in Appendix C that another fitting procedure of the data from Ref. 34, which, we believe, is more appropriate, is consistent with some k_z dispersion of the gap but no nodes on hole FSs. And the most recent synchrotron ARPES data³⁵ show no nodes on hole pockets and strong gap variation on electron pockets. It appears that more work is needed to resolve the structure of the gaps on hole and electron FSs in ARPES studies. From the theory viewpoint, a horizontal node on a hole FS is possible, 26 but less justified than nodes on electron pockets, as the latter appear quite naturally due to competition between interpocket repulsion between hole and electron pockets, which favors s^{+-} superconductivity, and intrapocket repulsion, which is against any superconductivity. The gap on electron pockets acquires $\cos 2\theta$ variations to reduce the effect of intrapocket repulsion and allow superconductivity to develop.^{7,15} This reasoning is consistent with the argument⁶ that a replacement of As by P changes the height of a pnictide with respect to the Fe plane, which effectively reduces interpocket electron-hole interaction, forcing the gap to develop nodes on electron pockets to reduce the effect of intrapocket repulsion. We therefore believe that nodes more likely reside on electron pockets, as we suggest in our analysis.

The structure of the nodes on electron pockets has been discussed in the context of the analysis of thermal conductivity data in BaFe₂(As_{1-x}P_x)₂. Measurements of the oscillations of thermal conductivity as a function of a direction of a magnetic field have been reported recently,²³ and the cos 4θ component of these oscillations has been interpreted using the same form of the gap on electron pockets as in our study: $\Delta(k_z) = \Delta[1 \pm \alpha(k_z)\cos 2\theta]$. The best fit to the data yields $\alpha(k_z) > 1$ for k_z near 0 and π and $\alpha(k_z) < 1$ for k_z near $\pi/2$. This form of $\alpha(k_z)$ implies that nodes form vertical loops centered at $k_z = 0$ and $k_z = \pi$. This is precisely what we found in our calculations. We therefore argue that our calculation provides microscopic explanation of the appearance of vertical loop nodes in BaFe₂(As_{1-x}P_x)₂.

VI. CONCLUSION

To conclude, in this paper we considered how the originally nodal s^{+-} gap changes if we include into the effective tight-binding model for Fe atoms an additional term with momentum transfer $(\pi,\pi,0)$ in 1111 systems and (π,π,π) in 122 systems. We show that such a term is generally present because the hopping between Fe orbitals is primarily an indirect hopping via pnictogen (chalcogen) orbitals, and pnictogen (chalcogen) atoms are located above and below the Fe plane in a checkerboard order. In 122 systems this order flips between neighboring Fe planes along the z axis. This additional hopping term hybridizes the two electron pockets and affects the gap structure. We found that the pairs of neighboring nodes (points where the quasiparticle energy is zero below T_c) approach each other as hybridization increases and disappear once the hybridization parameter λ exceeds

a certain threshold λ_c . We argued that in 122 systems, like BaFe₂(As_{1-x}P_x)₂, the threshold value depends on k_z and is much smaller near $k_z = \pi/2$ than near $k_z = 0$ and π . In this situation, at intermediate λ , the gap nodes form vertical loops which are centered at $k_z = 0$ and π and close up before reaching $k_z = \pi/2$.

We also found that in k_z cross sections where the nodes are present, they are located away from the hybridized FSs. As a result, at a nodal point, the peak in the ARPES energy distribution curve shifts, upon cooling through T_c , from a negative frequency to a smaller frequency. We showed that the nodes are surrounded by the no-shift lines—the subset of k points at which the ARPES peak does not shift between $T > T_c$ and $T < T_c$. These lines initially form beams along the directions where the s^{+-} gap vanishes, but they rapidly evolve as λ increases, and for $\lambda \lesssim \lambda_c$ form banana-shaped loops in the (k_x, k_y) plane around the nodes. We propose to search for these no-shift lines in ARPES measurements.

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APPENDIX A: MICROSCOPIC MECHANISM OF HYBRIDIZATION

In this Appendix we present microscopic derivation of Eq. (3) and obtain explicit expressions for $\lambda(k)$ in terms of microscopic parameters. We assume, following earlier works, that the hopping between Fe atoms occurs via pnictogen/chalcogen. Such a process gives rise to two types of Fe-Fe hopping terms: the ones with zero momentum transfer and the ones with momentum transfer Q. The terms with zero momentum transfer [and the ones with momentum transfer Q between fermion states near the center and the corners of the 1-Fe BZ (Ref. 11)] give rise to the electronic structure with hole and electron pockets. We assume that these terms are already incorporated into the tight-binding Hamiltonian of Eq. (1), and focus only on the terms with momentum transfer Q, which involve fermions with momenta near $(0,\pi)$ or $(\pi,0)$ and give rise to Eq. (3).

Equation (3) implies that

$$\lambda_{\mathbf{k}} = \langle \psi_{1,\mathbf{k}} | H | \psi_{2,\mathbf{k}+\mathbf{o}} \rangle, \tag{A1}$$

where H is the full hopping Hamiltonian. The band operators $\psi_{1,k}$ and $\psi_{2,k+Q}$ are linear combinations of atomic orbital operators. We consider d_{xz} , d_{yz} , and d_{xy} orbitals, and neglect d_{z^2} and $d_{x^2-y^2}$ orbitals which do not contribute to the states near the Fermi level.⁸ Let $|f_{s,n}\rangle$ denote orbital operators localized at site n with s=1,2,3 standing for d_{xz} , d_{yz} , and d_{xy} , respectively. The corresponding wave functions are shown in

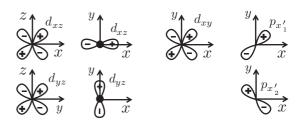


FIG. 6. Schematic representation of the three Fe orbitals d_{xz} , d_{yz} , d_{xy} , and p_x and p_y orbitals of As/Se.

Fig. 6. The band operators are

$$|\psi_{1,k}\rangle = \sum_{s=1}^{3} \gamma_{1}^{s}(\theta_{k})|f_{s,k}\rangle,$$

$$|\psi_{2,k+Q}\rangle = \sum_{s=1}^{3} \gamma_{2}^{s}(\theta_{k+Q})|f_{s,k+Q}\rangle,$$
(A2)

where

$$|f_{s,k}\rangle = \frac{1}{\sqrt{N}} \sum_{n} e^{ikn} |f_{s,n}\rangle.$$
 (A3)

The k-dependent coefficients $\gamma_1^s(\theta_k)$ [$\gamma_2^s(\theta_k)$] specify orbital contents of the pockets centered at $(0,\pi)$ or $(\pi,0)$, respectively, and are input parameters for our consideration.

Consider momentarily a single layer. We have $\mathbf{n} = (n,m)$ and $\mathbf{Q} = (\pi,\pi)$. Using

$$e^{i(k+Q)n} = (-1)^{n+m} e^{ikn},$$
 (A4)

we can separate the sums over n into contributions from even and odd sublattices, i.e., split \sum_{n} into $\sum_{n}' + \sum_{n}''$, where the first (second) sum is limited to even (odd) values of n + m. Equation (A2) then takes the form

$$|\psi_{1,k}\rangle = \frac{1}{\sqrt{N}} \left[\sum_{n}' + \sum_{n}'' \right] e^{ikn} \sum_{s=1}^{3} \gamma_{1}^{s}(\theta_{k}) |f_{s,n}\rangle,$$

$$|\psi_{2,k+Q}\rangle = \frac{1}{\sqrt{N}} \left[\sum_{n}' - \sum_{n}'' \right] e^{ikn} \sum_{s=1}^{3} \gamma_{2}^{s}(\theta_{k}) |f_{s,n}\rangle.$$
(A5)

Substituting (A5) into Eq. (A1) we obtain

$$\lambda_{k} = \frac{1}{N} \sum_{n'} \left[\sum_{n}' - \sum_{n}'' \right] e^{ik(n-n')}$$

$$\times \sum_{s,s'} \left[\gamma_{1}^{s}(\theta_{k}) \right]^{*} \gamma_{2}^{s'}(\theta_{k}) \langle f_{s',n'} | H | f_{s,n} \rangle. \quad (A6)$$

The sites within each sublattice are identical, hence $\langle f_{s',n'}|H|f_{s,n}\rangle$ depends only on n'-n. Introducing

$$A_{s's}^{l} = \langle f_{s',n+l} | H | f_{s,n} \rangle \quad n+m = 2p,
 A_{s's}^{l} = \langle f_{s',n+l} | H | f_{s,n} \rangle \quad n+m = 2p+1,
 (A7)$$

where p is an integer, we rewrite (A6) as

$$\lambda_{k} = \frac{1}{2} \sum_{l:s',s} \left(A_{s's}^{l} - A_{s's}^{\prime l} \right) e^{-ikl} \left[\gamma_{1}^{s}(\theta_{k}) \right]^{*} \gamma_{2}^{s'}(\theta_{k}). \tag{A8}$$

The summation in Eq. (A8) formally runs over all l but in reality does not extend beyond second neighbors. The same

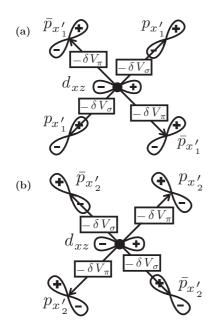


FIG. 7. The overlap integrals between iron orbital d_{xz} and inplane As/Se p_x and p_y orbitals are defined by two parameters δV_π and δV_σ . We show Fe atom from even sublattice, for which As/Se atoms are displaced off the Fe plane by $+\delta$ along the main diagonal (x=y), and by $-\delta$ along x=-y. The p-orbitals at $+\delta$ are labeled as p and the ones at $-\delta$ as \bar{p} . We assume that $\delta \ll 1$, in which case the overlap integrals are linear in δ . (a) overlap between d_{xz} and p'_{x_1} orbitals, (b) overlap between d_{xz} and p'_{x_2} orbitals.

expression is obtained in the 3D case, but then the sum over l extends to neighbors in the XY plane and along the z axis.

Equation (A8) expresses λ_k in terms of the band-structure parameters and hopping amplitudes. We see that the hybridization parameter is nonzero only if the hopping amplitudes are different for even and odd sublattices.

Further analysis requires the evaluation of the orbital hopping amplitudes and the knowledge of the orbital content of band operators. As we said, we neglect direct hopping between iron atoms and focus on a second-order tunneling processes via pnictogene/chalcogene. The amplitudes (A7) are then expressed in terms of hopping integrals from a d orbital on a Fe site to one of three p orbitals on a neighboring As/Se site. The p_z orbital has a much smaller overlap integral compared to the two in-plane orbitals, and we neglect it. The in-plane orbitals are presented in Fig. 6. Their wave functions are maximized in the direction along $x_1' = (x + y)/\sqrt{2}$ and $x_2' = (-x + y)/\sqrt{2}$, and we denote then by $p_{x_1',x_2'}$ and $\bar{p}_{x_1',x_2'}$ pnictogen/chlacogen above and below the iron plane, respectively.

Within the tight-binding approximation the hopping parameters between Fe and As/Se sites can be specified by a set of overlap integrals δV_{σ} and δV_{π} , as shown in Figs. 7 and 8. Here δ is the the deviation of the As/Se atom in an Fe plane. The wave functions of d_{xz} and d_{yz} orbitals change sign under $\delta \to -\delta$, hence the overlap integrals with p_{x_i} and \bar{p}_{x_i} have opposite signs.

In what follows we consider first the model with only d_{xz} and d_{yz} orbitals. We show that the hybridization parameter vanishes in a 2D case and in 3D systems for 1111 lattice structure, but is generally nonzero for 3D systems with 122

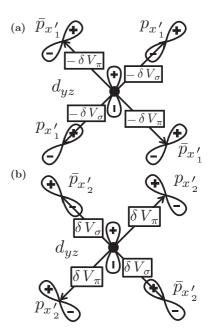


FIG. 8. Same as in Fig. 7 but for d_{yz} orbital of Fe. (a) Overlap between d_{yz} and $p_{x'_1}$ orbitals, (b) overlap between d_{yz} and $p_{x'_2}$ orbitals.

lattice structure, except special directions in k space where λ_k vanishes. We then include into consideration the d_{xy} orbital (i.e., consider the three-orbital model) and show that in this case the hybridization parameter is nonzero already in two dimensions and in 1111 systems. For 122 systems, λ_k in the three-orbital model is less anisotropic than in the two-orbital model and nonzero along all directions of k.

1. Two-orbital model

We follow earlier work¹⁸ and assume that the pocket at $(0,\pi)$ is predominantly made out of the d_{xz} orbital, and the one at $(\pi,0)$ is made out of the d_{yz} orbital, i.e., in our notations $\gamma_1^s(\theta_k) = \delta_{s,1}$ and $\gamma_2^s(\theta_k) = \delta_{s,2}$.

a. Single Fe layer

For a single iron layer, Eq. (A8) simplifies to

$$\lambda_{k} = \frac{1}{2} \sum_{l} \left(A_{2,1}^{l} - A_{2,1}^{\prime l} \right) e^{-ikl}, \tag{A9}$$

where, we remind, $A_{2,1}^l$ and $A_{2,1}^{nl}$ are hopping amplitudes from the d_{xz} orbital at site \boldsymbol{n} to the d_{yz} orbital at cite $\boldsymbol{n}+\boldsymbol{l}$ starting from \boldsymbol{n} at even or odd sublattice, respectively. Each amplitude describes a two-stage process: the electron first hops from the d_{xz} orbital to one of the two p orbitals of pnictogen/chalcogen, and then hops from this p orbital to d_{yz} orbital on either the first or second neighbor; see Fig. 9(a). Because both d_{xz} and d_{yz} orbitals are odd in z, elementary amplitudes of hopping from d to p have different sign for hopping originating from even and odd sites. However, taken to second order, the amplitudes $A_{2,1}^l$ and $A_{2,1}^{nl}$ turn out to be completely equivalent. We illustrate the equivalence in Fig. 9 for $\boldsymbol{l} = (1,1)$. As a consequence, $A_{2,1}^l = A_{2,1}^{nl}$, i.e., λ_k vanishes.

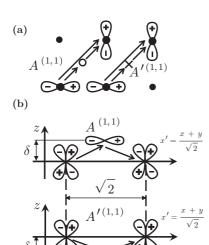


FIG. 9. The second-order hopping processes within a single iron layer shown as a top view (a) and a side view (b). The equality of the two amplitudes, $A^{(1,1)} = A^{r(1,1)}$, follows from the observation that both orbitals, d_{xz} and d_{yz} , are odd under the reflection $z \rightarrow -z$.

For completeness, we also computed the hybridization amplitude between d_{xz} and d_{yz} orbitals for Q = 0:

$$H_{1,2} = \sum_{\mathbf{k}} h_{1,2}(\mathbf{k}) f_1^{\dagger}(\mathbf{k}) f_2(\mathbf{k}). \tag{A10}$$

This term has been computed before⁸ and is part of the bare Hamiltonian which gives rise to hole and electron pockets. Using our method, we reproduce earlier result for $h_{1,2}$, as we now demonstrate.

Performing the same computations that for $Q = (\pi, \pi)$ lead to Eq. (A9), we obtain for Q = 0

$$h_{1,2} = \frac{1}{2} \sum_{l} \left(A_{2,1}^{l} + A_{2,1}^{\prime l} \right) e^{-ikl} . \tag{A11}$$

Because $A_{2,1}^{l} = A_{2,1}^{'l}$, Eq. (A11) becomes

$$h_{1,2} = \sum_{l} A_{2,1}^{l} e^{-ikl} \,. \tag{A12}$$

In the second order perturbation theory we have for, e.g., $l = (\pm 1, \pm 1)$ (see Figs. 7 and 8)

$$\begin{split} A_{2,1}^{(1,1)} &= A_{2,1}^{(-1,-1)} = -A_{2,1}^{(1,-1)} = -A_{2,1}^{(-1,1)} \\ &= \frac{\delta^2}{E_g} \left(V_{\sigma}^2 - V_{\pi}^2 \right), \end{split} \tag{A13}$$

where the energy denominator E_g is the energy separation between 3d to 4p orbitals. Substituting Eq. (A13) into Eq. (A12) we obtain

$$h_{1,2} = -4\frac{\delta^2}{E_a} (V_\sigma^2 - V_\pi^2) \sin k_x \sin k_y + \dots,$$
 (A14)

where dots stand for the contributions from other l. This result is in full agreement with earlier calculations, see e.g., Refs. 1,8, and 11.

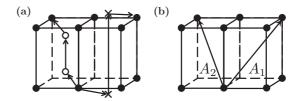


FIG. 10. Interlayer tunneling processes leading to a finite hybridization, (A15), in 122 material.

b. 3D crystals, 1111 materials

For 3D systems with 1111 structure, Fe layers at different z are all equivalent, and 3D folding vector $\mathbf{Q} = (\pi, \pi, 0)$. The arguments displayed in the previous section apply to this case as well, i.e., for two orbital model $\lambda_k = 0$, even if we include into consideration interlayer tunneling.

c. 3D crystals, 122 materials

In 122 materials with body-centered-tetragonal crystal structure the situation is qualitatively different. The first observation is that the hybridization vector is $\mathbf{Q} = (\pi, \pi, \pi)$ because even and odd sublattices are formed by Fe atoms located at $\mathbf{n} = (n, m, p)$ with n + m + p even or odd, respectively. This can be also be understood by noticing that the Fe-only lattice is simple cubic, but, because of As/Se, the Fe lattice has an fcc structure with the basis, or alternatively a rocksalt structure. The folding vector $\mathbf{Q} = (\pi, \pi, \pi)$ appears as an additional Bragg peak due to the transition from a simple cubic to an fcc lattice. Without interlayer tunneling, λ_k is still zero, but interlayer tunneling makes it finite as we show below.

Interlayer tunneling in real systems is a complex process which at least partly involves Ba atoms.¹⁷ We will avoid this complication and consider a toy model in which there is a direct tunneling between pnictogen/chalcogen atoms located at the same (x,y) in different layers. Because the position of pnictogen/chalcogen atoms relative to the Fe plane oscillates along the z direction, there are two different tunneling amplitudes for such processes: the one between pnictogen/chalcogen located above the nth plane and below the (n+1)th plane, and the other between pnictogen/chalcogen located below the nth plane and above the (n+1)th plane (see Fig. 10).

Another peculiarity of 122 systems is that the eccentricity of electron FSs in 122 systems changes sign between $k_z = 0$ and $k_z = \pi$, i.e., the FS at $(0, \pi 0)$ is elongated along the same direction as the FS at $(\pi,0,\pi)$. In the full model, this is due to the change of the relative weight of the d_{xy} orbital between $k_z = 0$ and $k_z = \pi$. In two-orbital approximation, we model the change of sign of eccentricity by requiring that d_{xz} and d_{yz} orbitals interchange between $k_z = 0$ and $k_z = \pi$ [i.e., we require that at $k_z = 0$, the pocket at $(0,\pi)$ is made out of the d_{xz} orbital and is elongated along the y axis, and the one at $(\pi,0)$ is made out of the d_{yz} orbital and is elongated along the x axis, while at $k_z = \pi$, the pocket at $(0,\pi)$ is made out of the d_{yz} orbital and is elongated along x, and the one at $(\pi,0)$ is made out of the d_{xz} orbital and is elongated along y]. The hybridization term with $\mathbf{Q} = (\pi, \pi, \pi)$ then connects the $(0, \pi)$ pocket at $k_z = 0$ and the $(\pi, 0)$ pocket at $k_z = \pi$, which have the same orbital character, i.e., s and s' in Eq. (A8) for λ_k are the same.

The process which gives rise to a nonzero λ_k is a three-stage process in which an electron from the d_{xz} or d_{yz} orbital on an even sublattice in layer n hops to one of two p orbitals on a pnictogen/chalcogen, then hops vertically to a pnictogen/chalcogen located near the next Fe layer, and then hops to the same d orbital on that layer. One can easily verify that the terms in λ_k in which do not cancel out between even and odd sublattices are the ones with $l = (\pm 1, \pm 1, \pm 1)$. There are two different hopping amplitudes for these momenta (see Fig. 10): for an even sublattice we have $A_{ss}^{(1,1,1)} = A_{ss}^{(1,-1,-1)} = A_{ss}^{(-1,-1,1)} = A_{ss}^{(-1,-1,1)} = A_{ss}^{(-1,-1,-1)} = A_{1}$, where s = 1,2, and for odd sublattice $A_{ss}^{(-1,1,1)} = A_{ss}^{(-1,-1,1)} = A$

$$\lambda_k = -4i(A_1 - A_2)\sin k_x \sin k_y \sin k_z. \tag{A15}$$

The expression (A15) is odd in all three momenta. This result is expected because the three reflection symmetries have been broken by hybridization. The overall factor of i reflects the fact that time-reversal symmetry is not broken (i.e., $\lambda_k = \lambda_{-k}^*$). For completeness, we also computed the hybridization term between d_{xz} and d_{yz} orbitals and found it is also nonzero, but this time λ_k is real and is an even function of k.

2. Three orbital model

We next consider how λ_k changes if we consider the more realistic situation when the d_{xy} orbital also contributes to the states near the FS.

a. 2D case

We use as an input the results of previous calculations, which found that the FS at $(0,\pi)$ is constructed out of d_{xz} and d_{xy} orbitals, and the one at $(\pi,0)$ is constructed out of d_{yz} and d_{xy} orbitals. To a reasonable approximation, $\gamma_1^1(\theta_k) = \sin\theta$, $\gamma_1^3(\theta_k) = \cos\theta$, and $\gamma_2^i(\theta) = \gamma_1^i(\pi/2 - \theta)$, where θ is counted from the y axis (as written, the formulas are valid in the first quadrant, for $0 < \theta < \pi/2$). Accordingly

$$\psi_{1,k} = f_{1,k} \sin \theta + f_{3,k} \cos \theta,
\tilde{\psi}_{2,k+Q} = f_{2,k+Q} \cos \theta + f_{3,k+Q} \sin \theta.$$
(A16)

The hybridization amplitude between $f_{1,k}$ and $f_{2,k+Q}$ vanishes, as we found before, but we show in this section that the amplitudes between $f_{1,k}$ and $f_{3,k+Q}$ and between $f_{3,k}$ and $f_{2,k+Q}$ are nonzero. In our notations, we then have

$$\lambda_k = \lambda_k^{3,1} + \lambda_k^{2,3},\tag{A17}$$

where

$$\lambda_k^{3,1} = \sin^2 \theta \sum_{l} \left(A_{3,1}^l - A_{3,1}^{\prime l} \right) \frac{e^{-ikl}}{2}$$
 (A18)

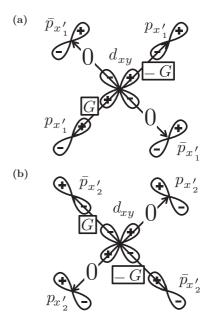


FIG. 11. Overlaps of iron d_{xy} orbital with As/Se orbitals $p_{x'_1}$ (a) and $p_{x'_2}$ (b). In case (a) the tunneling is possible only along the main diagonal direction, x = y, while in case (b) it occurs only along the perpendicular direction x = -y.

and

$$\lambda_k^{2,3} = \cos^2 \theta \sum_{l} \left(A_{2,3}^l - A_{2,3}^{\prime l} \right) \frac{e^{-ikl}}{2}.$$
 (A19)

Because the wave function for the d_{xy} orbital is even under the reflection $z \to -z$ and the ones for d_{xz} and d_{yz} orbitals are odd, $A_{3,1}^{\prime l} = -A_{3,1}^{l}$ and $A_{2,3}^{\prime l} = -A_{2,3}^{l}$. Equation (A19) then reduces to

$$\lambda_k = \sum_{l} \left(\sin^2 \theta A_{3,1}^l + \cos^2 \theta A_{2,3}^l \right) e^{-ikl}.$$
 (A20)

We now need to prove that this expression is nonzero. As before, we consider hopping between Fe sites as a two-stage process via neighboring p orbitals. This process gives rise to hopping to nearest- and next-nearest neighbors on the iron lattice, i.e., we need to consider $\mathbf{l} = (l_x, l_y)$ with $l_x, l_y = 0, \pm 1$. The overlap integrals with the p orbitals on As/Se have been defined in Figs. 7 and 8. In explicit form

$$\langle p_{x'_{1},\mathbf{n}+(1/2)(\hat{x}+\hat{y})} | H | f_{1,\mathbf{n}} \rangle = -\delta V_{\sigma},$$

$$\langle p_{x'_{2},\mathbf{n}+(1/2)(\hat{x}+\hat{y})} | H | f_{1,\mathbf{n}} \rangle = -\delta V_{\pi},$$

$$\langle \bar{p}_{x'_{1},\mathbf{n}+(1/2)(\hat{x}+\hat{y})} | H | f_{1,\mathbf{n}} \rangle = \delta V_{\sigma},$$

$$\langle \bar{p}_{x'_{1},\mathbf{n}+(1/2)(\hat{x}+\hat{y})} | H | f_{1,\mathbf{n}} \rangle = \delta V_{\pi},$$
(A21)

where, we remind, δ is the deviation of As/Se from an Fe plane. We define overlap integrals between d_{xy} and p orbitals in Fig. 11 as

$$\langle f_{3,n+\hat{x}}|H|p_{x'_{2},n+(1/2)(\hat{x}+\hat{y})}\rangle = G,$$

$$\langle f_{3,n+\hat{x}}|H|p_{x'_{1},n+(1/2)(\hat{x}-\hat{y})}\rangle = G,$$

$$\langle f_{3,n+\hat{x}}|H|\bar{p}_{x'_{2},n+(1/2)(\hat{x}+\hat{y})}\rangle = G,$$

$$\langle f_{3,n+\hat{x}}|H|\bar{p}_{x'_{1},n+(1/2)(\hat{x}-\hat{y})}\rangle = G.$$
(A22)

Other overlap integrals between d_{xy} and in-plane p orbitals vanish.

Using these notations, we obtain after a simple algebra

$$\begin{split} A_{3,1}^{(1,0)} &= \langle f_{1,n} | H \big| p_{x_2',n+(1/2)(\hat{x}+\hat{y})} \rangle \\ &\times \frac{1}{E_g} \langle p_{x_2',n+(1/2)(\hat{x}+\hat{y})} \big| H | f_{3,n+\hat{x}} \rangle \\ &+ \langle f_{1,n} | H \big| p_{x_1',n+(1/2)(\hat{x}-\hat{y})} \rangle \\ &\times \frac{1}{E_g} \langle p_{x_1',n+(1/2)(\hat{x}-\hat{y})} \big| H | f_{3,n+\hat{x}} \rangle, \end{split} \tag{A23}$$

$$A_{3,1}^{(1,1)} = \langle f_{1,n} | H | p_{x'_1,n+(1/2)(\hat{x}+\hat{y})} \rangle \times \frac{1}{E_g} \langle p_{x'_1,n+(1/2)(\hat{x}+\hat{y})} | H | f_{3,n+\hat{x}+\hat{y}} \rangle$$
 (A24)

and similar results for other $A_{3,1}^{(l_x,l_y)}$ and $A_{2,3}^{(l_x,l_y)}$. Substituting the expressions for the overlap integrals, Eqs. (A21) and (A22), we obtain

$$A_{3,1}^{(\pm 1,0)} = \mp \frac{2\delta V_{\pi} G}{E_{g}}, \quad A_{3,1}^{(0,\pm 1)} = 0,$$
 (A25)

$$A_{3,1}^{(\pm 1,\pm 1)} = \mp \frac{\delta V_{\sigma} G}{E_{\varrho}}, \quad A_{3,1}^{(\pm 1,\mp 1)} = \mp \frac{\delta V_{\sigma} G}{E_{\varrho}}, \quad (A26)$$

and similarly

$$A_{2,3}^{(0,\pm 1)} = \mp \frac{2\delta V_{\pi} G}{E_{\sigma}}, \quad A_{2,3}^{(\pm 1,0)} = 0,$$
 (A27)

$$A_{2,3}^{(\pm 1,\pm 1)} = \pm \frac{\delta V_{\sigma} G}{E_{g}}, \quad A_{2,3}^{(\pm 1,\mp 1)} = \mp \frac{\delta V_{\sigma} G}{E_{g}}. \quad (A28)$$

Substituting Eqs. (A25)–(A28) in Eq. (A20) and summing over four nearest- and four next-nearest neighbors, we obtain

$$\lambda_k = \frac{4i\delta G}{E_g} [V_\pi(\sin^2\theta \sin k_x + \cos^2\theta \sin k_y) + V_\sigma(\sin^2\theta \sin k_x \cos k_y - \cos^2\theta \sin k_y \cos k_x)].$$
(A29)

Introducing small $\tilde{k} = k - (0, \pi)$, using the fact that for a small-size pocket $\cos \theta = \tilde{k}_y/|\tilde{k}|$, $\sin \theta = \tilde{k}_x/|\tilde{k}|$, and $\sin k_x \approx \tilde{k}_x$, $\sin k_y \approx -\tilde{k}_y$, and extending the analysis to other quadrants (i.e., to negative \tilde{k}_x and \tilde{k}_y), we finally obtain

$$\lambda_{k} = \frac{4i\delta G}{E_{g}|\tilde{k}|^{2}} (V_{\pi} - V_{\sigma}) \left(|\tilde{k}|_{x}^{3} - |\tilde{k}|_{y}^{3} \right). \tag{A30}$$

We see that the hybridization parameter λ_k is generally nonzero, except for diagonal directions $\tilde{k}_x = \pm \tilde{k}_y$. This agrees with the result of numerical calculations.¹⁹ The authors of Ref. 19 found that in the presence of spin-orbit interaction $|\lambda|$ remains nonzero even along the diagonal directions.

b. 3D case

In 1111 systems the hybridization vector is $\mathbf{Q} = (\pi, \pi, 0)$, and for weak interlayer tunneling λ_k weakly depends on k_z and is nearly the same as in Eq. (A29). In 122 systems the hybridization vector is $\mathbf{Q} = (\pi, \pi, \pi)$, and the full expression for λ_k in the 3D case is the sum of the $d_{xz} - d_{yz}$ contribution, Eq. (A15), and the contribution from the processes involving

 d_{xy} , Eq. (A29). The two-orbital contribution is strongly k_z dependent, while the three-orbital contribution is k_z independent if we neglect interlayer hopping, and weakly depends on k_z if we include it. Because the two contributions vanish along different symmetry directions, the total hybridization parameter is nonvanishing for all k, though it has minima at $k_z = 0, \pi$, and along $k_x = \pm k_y$ and $k_x = 0, k_y = 0$ in a given cross section of k_z (k_x, k_y are measured with respect to the center of a pocket). The anisotropy of λ_k is further reduced if we add spin-orbit interaction. 17,19

APPENDIX B: EVOLUTION OF THE NODAL LINES AT SMALL HYBRIDIZATION

In this Appendix we discuss the initial evolution of the NSL from radial beams directed transverse to the FSs to tangential lines, directed along the FSs. We present the results for circular pockets. The evolution of the NSL for elliptical pockets is quite similar.

In the normal state, the dispersions for hybridized circular pockets are $\xi_k^{+-} = \xi_k \pm \lambda$, where $\xi_k = (k^2 - k_F^2)/(2m)$ is the dispersion in the absence of hybridization. In the superconducting state the dispersion is given by Eq. (12),

$$\omega_{1,2}^2(\mathbf{k}) = (\Delta^2 + y^2 \Delta^2 + \xi^2 + \lambda^2) \mp 2\sqrt{S},$$
 (B1)

where $S = \xi^2 \lambda^2 + y^2 \Delta^2 (\Delta^2 + \lambda^2)$ and $y = \alpha \cos 2\theta_k$. At $\lambda = 0$, Eq. (B1) reduces to a conventional expression $\omega_{1,2}^2(\mathbf{k}) = \xi^2 + \Delta^2 (1 \pm y)^2$. The dispersions in the normal and superconducting state coincide along four radial lines specified by $y = \pm 1$. Along these directions, the s^{\pm} gap has accidental nodes on one or the other electron FS.

Once λ becomes nonzero, the lines transform into bananatype loops still elongated transverse to the FS, and "domes" at $k > k_F$ [Fig. 12(a)] The loops close up at k = 0, and at $k = k_F$ and $y \approx \pm 1$. The NSL then undergo several topological changes at $\lambda \sim \Delta^2/\mu$, which is much smaller than critical $\lambda_c \sim \Delta$. At the first critical $\lambda = \lambda_{c,1}$ the bananas touch pairwise along the directions $\theta_k = 0$, $\pm \pi/2$ and π [Fig. 12(b)].

At larger λ , eight bananas transform into four configurations, which resemble rabbit ears [Figs. 12(c) and 12(d). The value of $\lambda_{c,1}$ is

$$\lambda_{c,1} \approx \frac{\Delta^2}{4\mu} \frac{(\alpha^2 - 1)^2}{\alpha^2 + 1}.$$
 (B2)

At the next critical

$$\lambda_{c,2} = \frac{\Delta^2}{4\mu} \tag{B3}$$

the "rabbit ears" touch each other along another set of symmetry directions, $\theta_k = \pm \pi/4$, $\pm 3\pi/4$ [Fig. 12(e)], and at $\lambda > \lambda_{c,2}$ detach from k = 0 [Fig. 12(f)]. The evolution of the NSL at larger $\lambda \sim \Delta$ is discussed in the main text and is shown in Fig. 4.

APPENDIX C: FITTING OF THE ARPES DATA

In this Appendix we discuss the fitting procedure used in Ref. 34 to extract the gap structure from ARPES data. The authors of this work symmetrized the measured photoemission intensity to get rid of Fermi function and extract the spectral

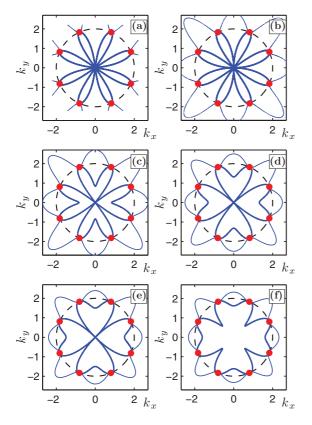


FIG. 12. (Color online) The initial evolution of the NSL defined as locus of points for which the fermion does not change its energy between the normal and the superconducting states. Dashed (black) lines show the FS before the hybridization. Thick (blue) lines are NSLs which are detectable by ARPES (the peaks above and below T_c are located at the same negative energy), thin (blue) lines are "nodal lines" for which the peak above T_c is at a positive energy. The hybridization parameter λ increases from (a) to (f). Dots (red) are nodal points at which quasiparticle energy is zero in a superconductor (but not in the normal state). Panel (a) $\lambda < \lambda_{c,1}$, panel (b) $\lambda = \lambda_{c,1}$, panels (c) and (d) $\lambda_{c,1} < \lambda < \lambda_{c,2}$, panel (e) $\lambda = \lambda_{c,2}$, panel (f) $\lambda > \lambda_{c,2}$. Both $\lambda_{c,1}$ and $\lambda_{c,2}$ scale as Δ^2/μ and are much smaller than $\lambda_c \sim \Delta$, at which the nodes disappear. The evolution at $\lambda \lesssim \lambda_c$ is shown in Fig. 3.

function $A(k,\omega) = (-1/\pi)G^{''}(k_F,\omega)$, and used the convention that the gap is finite when $A(k,\omega)$ at $k=k_F$ has two resolved maxima at finite frequencies, and zero when the maximum in the spectral function is at zero frequency. The same procedure was used earlier to identify Fermi "arcs" in the cuprates. This fitting procedure requires care because the maximum in $A(k_F,\omega)$ can be at zero frequency even when the gap is nonzero. This happens when fermionic damping is finite (as it always is at finite T, even in a conventional s-wave superconductor) and is larger than the gap.

To extract the gap from the data, the authors of Ref. 34 related the spectral function to fermionic self-energy in a standard way, as

$$A(k_F,\omega) = -\frac{1}{\pi} \frac{\Sigma^{''}(k_F,\omega)}{[\omega - \Sigma'(k_F,\omega)]^2 + [\Sigma''(k_F,\omega)]^2}$$
(C1)

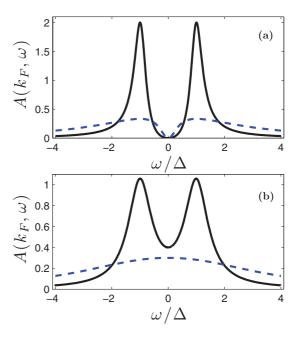


FIG. 13. (Color online) The spectral function $A(k_F,\omega)$ (a.u.), Eq. (C1), with self-energy given by (a) Eq. (C2) and (b) Eq. (C3). The solid black line is for $\gamma=0.5\Delta$. The dashed blue line is for $\gamma=3.0\Delta$. In case (a), the spectral function has a dip at $\omega=0$ and a peak at finite frequency for any nonzero Δ . In contrast, in case (b), the peak in the spectral function can be at $\omega=0$ despite that the gap is nonzero. This happens when the broadening is large enough, $\gamma>\sqrt{3}\Delta$. Notice that in this situation the peak at $\omega=0$ is very broad.

and modeled the self-energy at each k_z as

$$\Sigma(k_F,\omega) = -i\gamma + \frac{\Delta^2}{\omega}.$$
 (C2)

If one uses this fit, one finds that the maximum in the spectral function is at $\omega=0$ only when the superconducting gap vanishes [see Fig. 13(a)]. Indeed, the self-energy given by (C2) diverges at $\omega=0$ and therefore the spectral density has a dip at $\omega=0$ for any nonzero Δ . Because the measured spectral function α hole pocket is peaked at $\omega=0$ near $k_z=\pi$, the authors of Ref. 34 concluded that the gap on the α pocket must vanish for this k_z .

We argue that the fermionic self-energy of a dirty BCS superconductor contains the damping term $i\gamma$ not only as the stand-alone constant but also in the denominator of the Δ^2 term, along with ω , i.e., the true self-energy is

$$\Sigma_t(k_F,\omega) = -i\gamma + \frac{\Delta^2}{\omega + i\gamma}.$$
 (C3)

This form of the self-energy has been extensively discussed in the context of the physics of Fermi arcs in the cuprates. $^{37-39}$ Using this self-energy, one obtains that the spectral function has a maximum at $\omega=0$ even when the gap is finite, provided that $\gamma>\sqrt{3}\Delta$. We show in Fig. 13(b) that the spectral function obtained using the self-energy from Eq. (C3) with a nonzero Δ . We see that the maximum in $A(k_F,\omega)$ is either at a finite frequency or at $\omega=0$, depending on the interplay between Δ and γ . Observe that, when the maximum is at $\omega=0$, it is

quite broad, much like in the experimental data in Ref. 34 near $k_z = \pi$. We argue therefore that the data of the ARPES study

in Ref. 34 are in fact consistent with an anisotropic but still no-nodal gap along the α pocket.

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